## Cambridge IGCSE ${ }^{\text {TM }}$



You must answer on the question paper.
You will need: Geometrical instruments

## INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, center number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a calculator where appropriate.
- You may use tracing paper.
- You must show all necessary work clearly.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- For $\pi$, use either your calculator value or 3.142.


## INFORMATION

- The total mark for this paper is 104.
- The number of marks for each question or part question is shown in parentheses [ ].


## Formula List

| Area, $A$, of triangle, base $b$, height $h$. | $A=\frac{1}{2} b h$ |
| :--- | :--- |
| Area, $A$, of circle, radius $r$. | $A=\pi r^{2}$ |
| Circumference, $C$, of circle, radius $r$. | $C=2 \pi r$ |
| Lateral surface area, $A$, of cylinder of radius $r$, height $h$. | $A=2 \pi r h$ |
| Surface area, $A$, of sphere of radius $r$. | $V=4 \pi r^{2}$ |
| Volume, $V$, of prism, cross-sectional area $A$, length $l$. | $V=\pi r^{2} h$ |
| Volume, $V$, of cylinder of radius $r$, height $h$. | $V r^{3}$ |
| Volume, $V$, of sphere of radius $r$. |  |

1 (a) Using numbers from 55 to 85, write down
(i) a multiple of 23,
(ii) a factor of 120 ,
(iii) a common multiple of 8 and 12 ,
(iv) a number that is both square and odd,
(v) a number that has exactly 2 factors.
(b) Write 220 as the product of its prime factors.

2 (a) A cruise ship travels 2067 km .
(i) Write 2067 in words.
$\qquad$
(ii) Write 2067 correct to the nearest hundred.
(b) When full, the cruise ship carries 880 guests and 360 crew.

Write the ratio guests : crew in its simplest form.
$\qquad$ :
(c) There are 480 cabins on the ship.

On one cruise, 456 of these cabins were used.
Find the percentage of cabins that were used.
(d) Last year the cost of a cruise was $\$ 4600$.

This year the cost of the same cruise is $\$ 4784$.
Work out the percentage increase in the cost.
(e) The cost of building the ship was $\$ 153000000$.

Write 153000000 in scientific notation.
(f) There are 480 cabins on the ship.

There are four types of cabin: Ocean-view, Balcony, Interior, and Suite.
Hannah starts to draw a pie chart to show the numbers of each type of cabin.

(i) Show that there are 120 Ocean-view cabins on the ship.
(ii) The table shows information about each type of cabin.

| Type of cabin | Number of cabins | Sector angle in a pie chart |
| :--- | :---: | :---: |
| Ocean-view | 120 | $90^{\circ}$ |
| Balcony | 192 | $144^{\circ}$ |
| Interior | 68 |  |
| Suite | 100 |  |

(a) Complete the table.
(b) Complete the pie chart.

3 (a) Complete the table of values for $y=1+5 x-x^{2}$.

| $x$ | -1 | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ |  | 1 | 5 |  | 7 |  | 1 |

(b) On the grid, draw the graph of $y=1+5 x-x^{2}$ for $-1 \leqslant x \leqslant 5$.

(c) (i) On the grid, draw the line $y=3$.
(ii) Use your line to solve the equation $1+5 x-x^{2}=3$.

$$
x=. . . . . . . . . . . . . . . . . . ~ o r ~ x=
$$

4 (a) The diagram shows the plan of part of Rachel's garden.


Calculate the area.
$\qquad$ $\mathrm{m}^{2}$
(b) Rachel has a pond in her garden in the shape of a circle.

The circumference of the pond is 4.25 m .
Calculate the diameter of the pond.
Give your answer in centimeters.
(c) A plant pot is a cylinder with radius 15 cm and height 24 cm .

Calculate the volume of the pot.
(d) The diagram shows two mathematically similar plant pots.


The smaller pot has height 21.6 cm and diameter 27 cm .
The larger pot has diameter 33 cm .
Find the height, $h$, of the larger pot.

$$
h=\text {........................................... cm [2] }
$$

(e) A shop sells bags of compost in three different sizes.

| Small |
| :---: | :---: |
| 30 liters |
| $\$ 5.82$ | \left\lvert\, | Medium |
| :---: | :---: |
| 50 liters |
| $\$ 9.45$ | | Large |
| :---: |
| 75 liters |
| $\$ 14.50$ |\right.

Work out which size of bag gives the best value. Show how you decide.

5 The table shows the maximum power, kW , and the time taken, in seconds, to accelerate from 0 to $100 \mathrm{~km} / \mathrm{h}$ for each of 10 cars.

| Maximum <br> power (kW) | 77 | 52 | 103 | 55 | 44 | 51 | 85 | 135 | 90 | 110 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Time <br> (seconds) | 12.5 | 14.9 | 9.0 | 12.1 | 14.4 | 12.9 | 10.0 | 7.1 | 11.0 | 9.4 |

(a) (i) Find the range of the times.
(ii) Find the median maximum power.
kW [2]
(b) (i) Complete the scatter diagram.

The first eight points have been plotted for you.

(ii) What type of correlation is shown on the scatter diagram?
(iii) Describe the relationship between the maximum power of a car and the time taken to accelerate from 0 to $100 \mathrm{~km} / \mathrm{h}$.
$\qquad$
$\qquad$
(iv) Draw a line of best fit on the scatter diagram.
(v) Another car has a maximum power of 63 kW .

Use your line of best fit to estimate the time taken for this car to accelerate from 0 to $100 \mathrm{~km} / \mathrm{h}$.
(c) Robert buys a car for $\$ 18160$.

He pays a deposit of $\$ 6460$.
He pays the rest of the money in 24 equal monthly payments.
Work out the amount of each monthly payment.
\$
(d) A fuel tank holds 52 liters when full.

The tank is a quarter full.
Jim fills the tank with fuel that costs $\$ 0.85$ per liter.
Work out how much Jim pays.
\$

6 (a)

(i) On the grid, draw the image of
(a) triangle $A$ after a translation by the vector $\binom{3}{-7}$,
(b) triangle $A$ after a reflection in the line $x=3$.
(ii) Describe fully the single transformation that maps triangle $A$ onto triangle $B$.
$\qquad$
$\qquad$
(iii) Describe fully the single transformation that maps triangle $A$ onto triangle $C$.
$\qquad$
$\qquad$
(b)

(i) Write down the coordinates of the midpoint of the line $P Q$.
$\qquad$
(ii) Find the vector $\overrightarrow{Q P}$.

$$
\begin{equation*}
\overrightarrow{Q P}=( \tag{2}
\end{equation*}
$$

(iii) Point $R$ has coordinates $(6,-2)$ and $\overrightarrow{R S}=\binom{-4}{5}$.

Find the coordinates of point $S$.
$\qquad$

7 (a) $W=3 a+5 c$
Find the value of $W$ when $a=6$ and $c=2$.

$$
\begin{equation*}
W= \tag{2}
\end{equation*}
$$

(b) Factor completely.

$$
12 b+8 b^{2}
$$

(c) Solve for $m$.

$$
y=4 m-p
$$

$$
m=
$$

(d) Find the value of $x$ when $5^{x} \times 5^{3}=5^{12}$.

$$
x=
$$

(e) Find the value of
(i) $3^{0}$,
(ii) $5^{-2}$.
(f) In this part, all measurements are in centimeters.


NOT TO
SCALE

The diagram shows a kite with sides $(2 x+5)$ and $(3 x-1)$.
The perimeter of the kite is 33 cm .
Work out the length of a shorter side.

8 (a)

$P$ and $Q$ are points on the circle, center $O$.
$A P B$ is a tangent to the circle at $P$.
(i) Write down the mathematical name for the line $P Q$.
(ii) Explain why angle $O P B$ is $90^{\circ}$.
$\qquad$
(iii) Find the value of $x$.

$$
x=
$$

(b)


NOT TO
SCALE

The diagram shows two parallel lines and two straight lines.
(i) Find the value of $a$.

Give a reason for your answer.
$a=$ $\qquad$ because
(ii) Find the value of $b$.

Give a reason for your answer.
$b=$ $\qquad$ because
(iii) Find the value of $c$.

$$
c=
$$

(c)


Calculate the value of $x$.

$$
\begin{equation*}
x= \tag{3}
\end{equation*}
$$

9 A sequence of patterns is made using black counters and white counters.


Pattern 1
Pattern 2
Pattern 3
Pattern 4
(a) Draw Pattern 4.
(b) Complete the table.

| Pattern | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of black counters | 4 | 6 | 8 |  |  |
| Number of white counters | 1 | 4 | 9 |  |  |

(c) Write an expression, in terms of $n$, for
(i) the number of black counters in Pattern $n$,
(ii) the number of white counters in Pattern $n$.
(d) Elena has 30 black counters and 140 white counters.

Can she make Pattern 12 using her counters? Explain your answer.
because
$\qquad$

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